

New generation current sources

for unconditionally reliable very-low resistance measurements

Measurements of very-low resistances at cryogenic conditions are extremely demanding and frequently accompanied by common mode errors. As a rule, in presence of common mode errors, measurements of the same sample provide different results if

- performed in *different apparatuses*, or
- *different instrument types and models* are used for the resistance measurement *at the same sample installation* (i.e. the same cryostat and wiring), or
- *different instruments of the same model* are used for the resistance measurement *at the same sample installation.*

Common mode voltage signals can easily cause artificial experimental results. For example, the R(T) dependence of a superconductor in the vicinity of T_c exhibits a non-zero resistance in the superconducting state (either positive or negative) as a consequence of common mode voltage.



New patented technology (U.S. #9,285,809, March 2016): "Current source with active common mode rejection"

- enables the exact solution of common-mode issues in resistance measurements
- shifts reliability limits of very-low resistance measurements to the edge of physical limitations

AMS220 Voltage Controlled Current Source

is the only instrument on the market using the patented "active common mode rejection" technology,

- ensures active rejection of common mode voltage in resistance measurements,
- allows routine measurements of very low resistances (less than 1mΩ), even in the most demanding conditions (e.g. at temperatures below 500mK).



The AMS220 in conjunction with a lock-in amplifier represents a favorable replacement for an AC resistance / impedance bridge.



Very-low resistance measurements: How to ensure reliable results?

Measurements of low-level signals are frequently affected by common mode errors

The four-wire (Kelvin) method is used to measure low resistances because *it helps to eliminate errors due to lead and contact resistances*. However, its use does not guarantee the correct result of very-low resistance measurements. In a typical four-wire resistance measurement as illustrated in Fig.1, the test current (I_{τ}) is forced through the resistance (R_{τ}) being measured, and the voltage across the test resistance (V_{ρ}) is sensed. The measured resistance is

$$R_{\tau} = V_{D} / I_{\tau}$$

but in a real measurement the resistance is determined as

 $R_{\tau} = V_{M} / I_{\tau},$

where $V_{_{M}}$ is the value provided by the voltmeter sensing the voltage $V_{_{D}}$. If the input impedance of the voltmeter is sufficiently high, the effect of the sense current (I_s) can be neglected. But still, especially at very-low resistance measurements, $V_{_{M}}$ often differs from $V_{_{D}}$ due to *common mode error*, even if high-precision instruments *capable to measure very small voltage differences* (e.g. lock-in amplifiers) are used.

The value $V_{_{M}}$ is based on a processing of an output voltage signal (V_o) of a differential amplifier (operating with a differential gain G_o) at the input of the voltmeter. The output voltage of an *ideal differential amplifier would be* $V_o^{_{ideal}} = G_o V_o$. However, if the voltage difference that appears across two inputs of the differential amplifier, $V_{+} - V_{-} = V_{_{D}}$, is much less then the common mode voltage $V_{_{CM}} = (V_{+} + V_{-})/2$ (i.e. $V_o < V_{_{CM}}$), then V_o can significantly differ from $V_o^{_{ideal}}$. In this case, contribution coming from the common mode voltage has to be considered, and the output voltage can be expressed by the equation

$V_{o} = G_{D}(V_{+} - V_{-}) + G_{CM}(V_{+} + V_{-})/2 = G_{D}V_{D} + G_{CM}V_{CM},$

where G_{cM} is the common mode gain.

The ratio $G_o / |G_{cM}|$ (so-called common mode rejection ratio, CMRR) characterizes the extent to which the common mode voltage is rejected by the differential amplifier. The CMRR can be expressed also in decibels, being then referred to as common mode rejection (CMR); CMR = $20\log_{10}$ CMRR.



Fig. 1 Depiction of a typical four-wire resistance measurement with a block diagram of the signal processing by the voltmeter.

The CMR of an instrument/device is its key specification indicating how much of the common mode signal will appear in the measurement. In fact, limiting capability of instruments to reject common mode signals represents serious limitations for very-low resistance measurements (including those performed by means of Kelvin method), such as resistances in the current path can cause common mode voltage, which can be even several orders of magnitude greater than the sensed voltage (V_p). Nowadays technology limit is approximately 140 dB (CMRR = 10⁷, i.e. amplification of the differential voltage across the amplifier inputs is 10 million times greater than the amplification of the common mode signal). Typically, the CMR varies between 80 dB (CMRR = 10⁴) and 120 dB (CMRR = 10⁶).

Common mode errors in "standard" four-wire resistance measurements

Let us imagine measuring the resistance of a 100 $\mu\Omega$ test resistor as illustrated in Fig. 2. If current of 10 mA is forced through this resistor, the voltage across the resistor is $V_p = 1 \mu V (100 \mu\Omega \times 10 mA = 1 \mu V)$. Let us consider use of a current source with one of the outputs connected to the signal ground (single-ended current source). If the resistance of the current path connected to the grounded output is $R_{IB} \approx 20\Omega$, the common mode voltage $V_{CM} \approx 20\Omega \times 10 mA = 200 mV$ will be created in such experimental setup. Note that this value is much greater than V_p . At using an industry standard lock-in amplifier with CMR $\approx 100 dB$ (i.e. CMRR $\approx 10^5$) to sense the voltage, the corresponding common mode error is ≈ 200 mV /10⁵ = 2 μ V, thus the value provided by the lock-in amplifier, being a sum of V_p (1 μ V) and the common mode error (2 μ V), is **3\muV instead of 1\muV**. Correspondingly, the resistance gained from the experiment is **300** $\mu\Omega$ **instead of 100** $\mu\Omega$.



Fig. 2 Four-wire resistance measurement setup with a current source with one of the current outputs connected to the signal ground. The indicated measured value (affected by common-mode error) is illustrative with regard to the discussed example.

How to identify common mode errors in resistance measurements

A simple test to identify common mode errors in four-wire resistance measurement can be done by modification of an original four-wire resistance measurement setup as shown in Fig. 3a to one from Fig. 3b. Because in this case both voltage inputs (V_A, V_B) sense the same electrical signal, the sensed voltage difference is zero, so the correct resistance measurement must **unconditionally give a value of 0** Ω .



Fig. 3 Tests to identify common mode errors. Schematic depiction of the standard four-wire resistance measurement setup (a), its modification for the simplified test (b), and connection for the thorough test (c). When the purpose of the thorough test is to check a measuring instrument, without testing a complex wiring, the resistance under test can be replaced by a shortcut.

However, this simplified test yields information relevant only to the particular experimental conditions (particular load, specific temperature, etc.), but it does not necessarily reveal possible system weaknesses in all cases where the setup can be used. For example, it can be insufficient for systems where the resistance of current paths (i.e. resistance of current leads or contact resistances) vary significantly due to temperature changes. This simple test can also be conditionally ineffective when using socalled differential current sources. Differential current sources drive the load "symmetrically", i.e. voltage on their outputs I, and I_s is of the same absolute value but of the opposite polarity. Thus, if both current branches have equal resistances, the common mode voltage is zero, and so the common mode error is also zero in this specific case. However, when this balance is broken, e.g. by different contact resistances, potentials of voltage signals sensed on the test resistance move towards the potential of the output connected with the branch of lower resistance, which results in a creation of common mode voltage. This causes corresponding common mode error that increases with imbalance increase.

A thorough test can be performed using the connection shown in Fig. 3c., containing resistors that can be used to change the resistance of the electric current path by means of the switches S_A and S_B . Resistances (R_A and R_B) of these resistors should be comparable to resistances of current path branches (R_{IA} , R_{IB}) in a real experiment, and should not be less than the estimated maximum resistance change of the current path that may occur in (different) experiments. Detailed inspection shall be performed by measuring all combinations possible to be created by the switches S_A and S_B . A properly measuring system must unconditionally provide a value of 0 Ω for any combinations of R_{IA} and R_{IB} . Fig.4 shows examples how the results of the test can look like if $R_A = R_B = 10 \Omega$, and the CMR of the voltage sensing unit is 100 dB.



Fig. 4 Possible common mode errors for a single-ended (a) and a differential (b) current source. A settling time of an instrument is represented by intervals between steady readings.

Results of the test as shown in Fig. 4 can be estimated for different CMR of an instrument^{*)} using the table below if $R_A = R_B = 10 \Omega$. Note that the higher the resistance values R_A and R_B , the higher the common-mode errors.

CMR [dB]	80	90	100	110	120	130	140
R s-ε [μΩ]	1000	316	100	31.6	10	3.16	1
R_{DIF} [μΩ]	500	158	50	15.8	5	1.58	0.5

^{*)} The CMR depends on frequency and instrument settings. For instance, the CMR of a lock-in amplifier is less for AC coupling than for DC one. Manufacturers usually specify the CMR for DC coupling.

Overcoming the common mode errors in four-wire resistance measurements

Let us imagine measuring the resistance of a 100 $\mu\Omega$ test resistor with the use of the current source with active common mode rejection as illustrated in Fig.5. The circuit of active common mode rejection (ACTIVE CMR) monitors the voltage sensed by the inputs (V_{av} , V_{b}) of the voltage sensing device and using a feedback loop regulates the voltage at current outputs in order to achieve that common mode voltage of the monitored signals is zero ($V_{cM} \rightarrow 0V$). Thanks to the patented technology the component of V_{cM} originating in the lead and contact resistances in the current path can be suppressed to less than few microvolts. It can be estimated that with the use of measuring device with CMR \approx 100dB, or greater, **the common mode error can be eliminated to the level of tens of picovolts, or less!** The AMS220 is the only instrument on the market possessing the patented technology of active common mode rejection.



Fig. 5 Four-wire resistance measurement setup utilizing current source with active common mode rejection ($^{\prime }$ U.S. Patent #9,285,809)

AMS220 Voltage Controlled Current Source

with Active Common Mode Rejection



... for lock-in amplifier users performing very-low resistance measurements in the most demanding conditions

FEATURES

- Patented common-mode rejection technology
- Output current to ±50 mA •
- Voltage-to-current conversion ranges from $1 \mu A/V$ to 10 mA/V
- ±5 V control voltage input range •
- Low-noise, all analog design
- Optimized for use with lock-in amplifiers
- Easy to use with DAQ devices

TARGETED APPLICATIONS

- **Replacement for AC resistance bridges when used** • with lock-in amplifiers
 - Very-low resistance measurements down to mK temperatures
 - Superconductivity research
 - Hall effect phenomena
 - Higher harmonic detection in resistance measurements
 - Thermometry/calorimetry
 - Mutual inductance measurements
- AC and DC electrical measurements with DAO devices
 - Cost-effective solution for resistance measurements and thermometry
 - I-V curves measurements
- **Replaces floating current sources in resistance** measurements

Basic specifications

Ranges of voltage-to-current conversion:	0.001, 0.01, 0.1, 1, 10 [mA /V]			
Control voltage input range:	3.6 V _{RMS} / ±5 V _{DC}			
Maximum AC/DC output current:	36 mA _{RMS} / ±50 mA _{DC}			
Targeted frequency range:	DC - 200 Hz @ 'ACTIVE CMR' operation mode ENABLED			
	DC - 20 kHz (2 kHz for 1µA/V range) @ 'ACTIVE CMR' operation mode DISABLED			
Power:	12 V (AC, 50-60 Hz) / 0.6 A			

Manufacturer

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